Indian Institute of Technology Patna Department of Electrical Engineering

EE549 - Power System Dynamics and Control

Spring - 2022 End Semester Exam April 27, 2022

Time: 3 Hour Marks: 50

The DAE (Differential Algebraic Equations) of the flux decay model excluding exciter dynamics are

$$T'_{d0} \frac{dE'_q}{dt} = -E'_q - (X_d - X'_d)I_d + E_{fd}$$

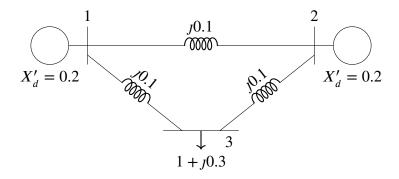
$$\frac{d\delta}{dt} = \omega - \omega_s$$

$$\frac{2H}{\omega_s} \frac{d\omega}{dt} = T_m - T_e - D(\omega - \omega_{base})$$

$$V_q + R_s I_q = -X'_d I_d + E'_q$$

$$V_d + R_s I_d = X_q I_q$$

1. The voltage at the node 3 is 0.98∠10°. Reduce the bus admittance matrix. Assume the load is of constant impedance type.



2. Consider a SMIB system.

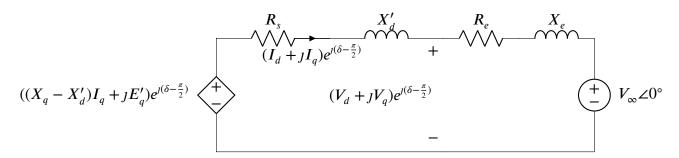


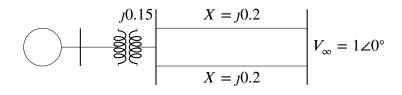
Figure 1: Synchronous Machine Flux Decay Model

- (a) Determine T_e .
- (b) Express T_e in terms of δ and E'_a .
- 3. Consider a SMIB system. The synchronous generator is represented using the flux decay model. The generator parameters are as follows:

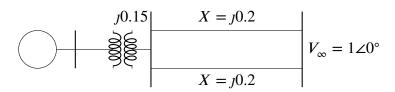
$$X_d = 1.8$$
 $X_q = 1.7$ $X_d' = 0.17$ $R_a = 0.003$ $T_{do}' = 0.4$ s $H = 4$ $D = 0$

If the terminal conditions are

$$P_t = 1.0 \quad |V_t| = 1.0$$



- (a) Find the initial conditions.
- (b) Prove that $T_e = P_t + I_a^2 R_a$.
- 4. Consider a SMIB system. The synchronous generator is represented using the classical model.



The generator parameters are as follows:

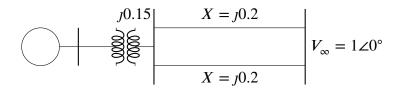
$$X'_d = 0.3$$
 $H = 3.5$ $D = 0$ $f = 60$ Hz

If the prefault system conditions are

$$P_t = 1.0 \quad |V_t| = 1.0$$

Analyze the transient stability of the system for a solid three phase fault at the sending end on one of the transmission lines. The fault is cleared by simultaneously opening the circuit breakers at both ends of the line.

- (a) Determine the critical clearing angle and time using the Equal Area Criterion.
- (b) Verify it using the energy function method.
- 5. Consider a SMIB system. The synchronous generator is represented using the classical model.



The generator parameters are as follows:

$$X'_d = 0.3$$
 $H = 3.5$ $D = 0$ $f = 60$ Hz

Analyze the small signal characteristics of the system about the steady operating condition following the loss of one line. The post fault system conditions at the machine terminal are

$$P_t = 1.0 \quad |V_t| = 1.0$$

- (a) determine the time response of δ if $\Delta \delta = 5^{\circ}$
- (b) determine the time response of ω if $\Delta \omega = 0$